

Day 5 - Simplifying Radicals with Variables - Notes

When simplifying radical expressions, you simplify the variables using the same method as you did previously (Remember $\sqrt{x^2} = x$; square and square roots undo each other).

a. $\sqrt{x^8}$

$$\sqrt{\overbrace{x \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x}^{\text{circled}}}$$

$$\downarrow \downarrow \downarrow \downarrow$$

$$x \cdot x \cdot x \cdot x$$

$$x^4$$

b. $\sqrt{x^5}$

$$\sqrt{\overbrace{x \cdot x \cdot x \cdot x \cdot x}^{\text{circled}}}$$

$$\downarrow \downarrow$$

$$x \cdot x \cdot \sqrt{x}$$

$$x^2 \sqrt{x}$$

c. $\sqrt{y^4 z^3}$

$$\sqrt{\overbrace{y \cdot y \cdot y \cdot y \cdot z \cdot z \cdot z}^{\text{circled}}}$$

$$\downarrow \downarrow \downarrow$$

$$y \cdot y \cdot z \sqrt{z}$$

$$y^2 z \sqrt{z}$$

Simplifying Radical Expressions with Square Roots

When simplifying radical expressions, you simplify both the coefficients and variables using the same method as you did previously (Remember $\sqrt{x^2} = x$; square and square roots undo each other). Remember, anything that is left over stays under the radical!

a. $\sqrt{9x^6}$ ^{P.S.}

$$\boxed{3x^3}$$

b. $\sqrt{4x^4}$ ^{P.S.}

$$\boxed{2x^2}$$

c. $\sqrt{32z^7}$

$$\sqrt{\overbrace{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot z \cdot z \cdot z \cdot z \cdot z}^{\text{circled}}}$$

$$2 \cdot 2 \cdot z \cdot z \cdot z \sqrt{2z}$$

$$\boxed{4z^3 \sqrt{2z}}$$

d. $\sqrt{45y^2}$

$$\sqrt{\overbrace{3 \cdot 3 \cdot 5 \cdot y \cdot y}^{\text{circled}}}$$

$$\boxed{3y\sqrt{5}}$$

e. $2\sqrt{27a^4b}$

$$2 \cdot \sqrt{\overbrace{3 \cdot 3 \cdot 3 \cdot a \cdot a \cdot a \cdot a \cdot b}^{\text{circled}}}$$

$$2 \cdot 3 \cdot a \cdot a \cdot \sqrt{3b}$$

$$\boxed{6a^2 \sqrt{3b}}$$

f. $3\sqrt{12x^2}$

$$3 \cdot \sqrt{\overbrace{2 \cdot 2 \cdot 3 \cdot x \cdot x}^{\text{circled}}}$$

$$3 \cdot 2 \cdot x \sqrt{3}$$

$$\boxed{6x\sqrt{3}}$$

g. $3\sqrt{18a^4}$

$$3 \cdot \sqrt{\overbrace{2 \cdot 3 \cdot 3 \cdot a \cdot a \cdot a \cdot a}^{\text{circled}}}$$

$$3 \cdot 3 \cdot a \cdot a \sqrt{2}$$

$$\boxed{9a^2 \sqrt{2}}$$

h. $-2\sqrt{36f^3g^4}$ ^{P.S.}

$$-2 \cdot 6 \sqrt{\overbrace{f \cdot f \cdot f \cdot g \cdot g \cdot g \cdot g}^{\text{circled}}}$$

$$\boxed{-12fg^2 \sqrt{f}}$$

i. $5\sqrt{20x^{16}y^{10}}$

$$5 \cdot \sqrt{\overbrace{2 \cdot 2 \cdot 5 \cdot x^{16} \cdot y^{10}}^{\text{circled}}}$$

$$5 \cdot 2 \cdot x^8 y^5 \sqrt{5}$$

$$\boxed{10x^8 y^5 \sqrt{5}}$$