

# Day 4 – Creating Function Rules – Notes

Learning Goal: I can create a function rule to describe a relationship. 0 1 2 3 4

Scenario: Consider the following situations...

- The number of hours worked and the money earned

I                      D

*Money earned depends on hours worked*

- Your grade on a test and the number of hours you studied

D                      I

*Your grade depends on how much you study.*

- The number of people working on a particular job and the time it takes to complete a job

I                      D

*The time it takes to complete depends how many people working*

- The total cost of a pizza delivery and the number of pizzas ordered

D                      I

*The total cost depends on how many pizzas you order*

- The speed of a car and how far the driver pushes down on the gas pedal

D                      I

*Speed of car depends on how much you push the pedal*

There are two quantities changing in each situation. When one quantity depends on the other in a problem situation, it is said to be the **dependent quantity**. The quantity that the dependent quantity depends on is called the **independent quantity**. When you have a function, the input value that represents the independent quantity is considered the **independent variable** and the output value that represents the dependent quantity is considered the **dependent variable**.

Independent Quantities/Variables	Dependent Quantities/Variables
Input values	Output values
Not changed by other quantities	Changes due to independent quantity
Located on x-axis	Located on y-axis

In the scenarios listed above, circle the independent quantity and underline the dependent quantity. Then name a variable to represent the independent and dependent quantities.



Creating Function Rules

Ex. Create a function rule for the tables below:

A.

x	1	2	3	4
y	-1	0	1	2

$$\begin{aligned}
 1 - 2 &= -1 \\
 2 - 2 &= 0 \\
 3 - 2 &= 1 \\
 4 - 2 &= 2 \\
 x - 2 &= f(x)
 \end{aligned}$$

$$f(x) = x - 2$$

B.

Time Worked (h) x	1	2	3	4
Amount Earned (\$) y	5	10	15	20

$$\begin{aligned}
 1 \times 5 &= 5 \\
 2 \times 5 &= 10 \\
 3 \times 5 &= 15 \\
 4 \times 5 &= 20 \\
 x \times 5 &= f(x)
 \end{aligned}$$

$$f(x) = 5x$$

C.  $\{(1, 3), (2, 6), (3, 9), (4, 12)\}$

$$\begin{aligned}
 1 \times 3 &= 3 \\
 2 \times 3 &= 6 \\
 3 \times 3 &= 9 \\
 4 \times 3 &= 12 \\
 x \times 3 &= f(x)
 \end{aligned}$$

$$f(x) = 3x$$

D.  $\{(1, -6), (2, -5), (3, -4), (4, -3)\}$

$$\begin{aligned}
 1 - 7 &= -6 \\
 2 - 7 &= -5 \\
 3 - 7 &= -4 \\
 4 - 7 &= -3 \\
 x - 7 &= f(x)
 \end{aligned}$$

$$f(x) = x - 7$$

E. A hot air balloon cruising at 1000 feet begins to ascend. It ascends at a rate of 200 feet per minute. Create a function  $f$  to represent the height of the balloon for  $m$  minutes. How many minutes does it take to reach 1400 feet?

$$f(x) = 1000 + 200x$$

$\downarrow$  height                       $\downarrow$  # of minutes

$$\begin{aligned}
 1400 &= 1000 + 200x \\
 -1000 &\quad -1000 \\
 \hline
 400 &= 200x \\
 \frac{400}{200} &= \frac{200x}{200} \\
 x &= 2
 \end{aligned}$$

It takes 2 minutes to reach 1400 ft.

F. A fish tank filled with 12 gallons of water is drained. The water drains at a rate of 1.5 gallons per minute. Create a function  $f$  to represent the number of gallons remaining after  $m$  minutes. How long does it take for the tank to have 3 gallons remaining?

$$f(m) = 12 - 1.5m$$

$\downarrow$  gallons remaining                       $\downarrow$  # of minutes

$$\begin{aligned}
 3 &= 12 - 1.5m \\
 -12 &\quad -12 \\
 \hline
 -9 &= -1.5m \\
 \frac{-9}{-1.5} &= \frac{-1.5m}{-1.5} \\
 m &= 6
 \end{aligned}$$

It takes 6 minutes to reach 3 gallons remaining.

Ex. Create a function rule for each person

Maya runs 7 miles per week and increases her distance by 1 mile each week. Matthew runs 4 miles per week and increases his distance by 2 miles each week.

a. Maya's Function Rule:

$$f(x) = 7 + x$$

$\downarrow$  total miles                       $\downarrow$  # of miles

b. Matthew's Function Rule:

$$g(x) = 4 + 2x$$

$\downarrow$  total miles                       $\downarrow$  # of miles

c. Who has run farther after 4 weeks?

Maya:  $f(4) = 7 + 4$   
 $f(4) = 11$

Matthew:  $f(4) = 4 + 2(4)$   
 $f(4) = 12$

Matthew has run 12 miles compared to Maya's 11 miles.